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In [2]: import numpy as np
from numpy import pi
# importing Qiskit
from qiskit import QuantumCircuit
from qiskit import ClassicalRegister, QuantumRegister
import matplotlib.pyplot as plt
```

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In [3]: def sim_sv(qc, text):
    """Get the statevector of the output of the circuit qc"""
    #import libs
    from qiskit_textbook.tools import vector2latex
    from qiskit import Aer, execute
    from qiskit.quantum_info import Statevector
    #code
    sv_sim = Aer.get_backend('statevector_simulator')
    sv = execute (qc, sv_sim).result().get_statevector()
    #vector2latex(sv, pretext = "/" + text + "\rangle =")
    return sv
```

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In [4]: def qft_rotations(circuit, n):
    """Performs qft on the first n qubits in circuit (without swaps)"""
    for i in range (n):
        circuit.h(i)
        m = 1
        for j in range (i+1,n):
            m = m +1;
            circuit.cu1(-2*pi/2**(m), i, j)
```

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In [5]: def swap_registers(circuit, n):
    for qubit in range(n//2):
        circuit.swap(qubit, n-qubit-1)
    return circuit
```

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In [6]: def makeQFTgate(N):
    """returns a gate of centred QFT, swaps qubits"""
    temp = QuantumCircuit (N)
    swap_registers(temp, N)
    qft_rotations(temp,N)
    temp.x(n-1);
    QFTC = temp.to_gate()
    QFTC.name = "QFT_" + str(N)
    return QFTC
```

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In [7]: def phase(n, phi):
    """returns the phase transformation gate for n qubits"""
    qc = QuantumCircuit(n+1);
    for i in range (n):
        qc.u1(phi/(2**(i+n-3)), n-1-i)
    for i in range (n):
        for j in range (i+1,n):
            qc.cx(n-1-j, n)
            qc.cx(n-1-i, n)
            qc.u1(phi* (2**(2-i-j)), n) #2-i-j or 4?
            qc.cx(n-1-i, n)
            qc.cx(n-1-j, n)
    phcirc = qc.to_gate()
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phcirc.name = 'phase'+str(phi)
return phcirc
```

```
In [16]: def evolve (n,phi,initial_state, stepsnumber):
          """returns the state vector after evolving the initial_state for stepsnumber times"""
          ## make the circuit
          n1 = n+1
          snaps = []
          m = 2**7
          #qubits
          for i in range (stepsnumber):
              q = QuantumRegister(n1)
              qc = QuantumCircuit(q)
              qc.barrier();
              #initialization
              magnitude = np.linalg.norm(initial_state)
              initial_state =initial_state/magnitude
              qc.initialize(initial_state, list(range(n)))
              qc.barrier();
              #gates
              QFT = makeQFTgate(n)
              phkinetic = phase (n,(i+1)*phi/m)
              QFTi = QFT.inverse()
              QFTi.name = "QFTi_" + str(n)
              phpotential = phase (n,((i+1)*16*phi/2/4)/m) ##16 to double the potential
              for j in range (m):
                  #QFT
                  qc.append(QFT,range(n))
                  qc.barrier();
                  #phase
                  qc.append(phkinetic,range(n+1))
                  qc.barrier();
                  #inverse QFT
                  qc.append(QFTi,list(range(n)))
                  qc.barrier()
                  ##another phase for the harmonic potential
                  qc.append(phpotential,range(n+1))
              finalstate = sim_sv(qc,'\psi')
              prob = np.square(abs(finalstate))
              snaps.append(prob)
          return snaps
```

```
In [17]: def action ():
          """plots the the snapshots of the evolution process"""
          snaps = evolve(n,phi,initial_state, stepsnumber)
          plt.plot(np.square(abs(initial_state)), 'r')
          leg = ["t=0"]
          plt.xlabel("x basis")
          plt.ylabel("relative prob.")
          for i in range (stepsnumber):
              plt.plot(snaps[i])
              leg.append("t="+ str(i+1)+ "$\Delta t$" + " = " + str(round((i+1)*phi/pi,2)) + " ")
          x=plt.axis([0, 2**n-1, 0, 1.1*max(np.square(abs(initial_state)))])
          plt.legend(leg)
```

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In [19]: ##commented are descriptions of parameters, and different intitial states to play with
          ##parameters
          n = 10; ## number of qubits
          phi = 200*pi; ##time of evolution
          ##width= 14*2; ## 14*2 works so well centered (splitted) non moving gaussian without x g
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        ## 15.2 + sqrt what works so well for coherent state oscillation with n =
        ## 15.2
width = 15.2/2; ## this is the correct width;
#initial_state = np.sqrt(np.exp(-(np.linspace(0,2**n-1, 2**n) - (2**n/2) +0.5)**2/(2*width**2)))
## ground state of harmonic oscillator # actually not an error sqrt of gaussian is gaus

#initial_state = (np.exp(-(np.linspace(0,2**n-1, 2**n) )**2/(2*width**2))) + (np.exp(-(
## removed the sqrt what an error

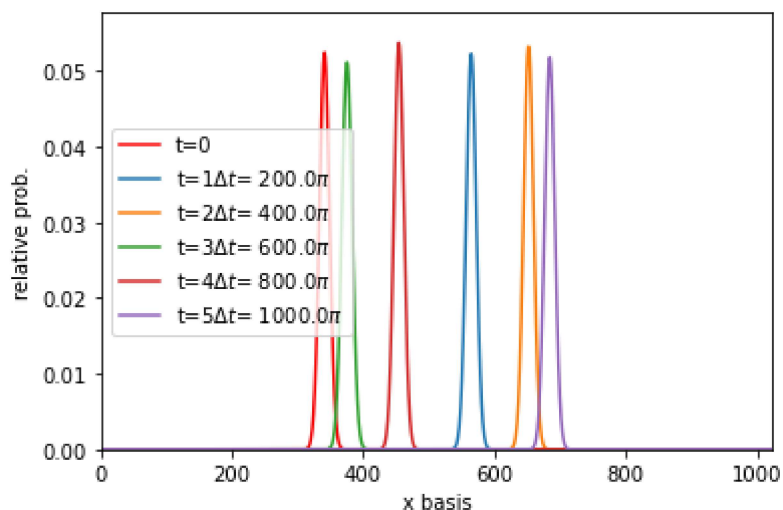
#initial_state = np.sqrt(np.exp(-(np.linspace(0,2**n-1, 2**n) - (2**n/3) +0.5)**2/(2*15
# coherent state
initial_state = np.sqrt(np.exp(-(np.linspace(0,2**n-1, 2**n) - (2**n/3) +0.5)**2/(2*width

##general energy state
#w=2 #harmonic
#mom = np.zeros(2**n);
#mom[w]=1
#mom [2**n-w]=1
#initial_state= np.fft.fft(mom,2**n)
magnitude = np.linalg.norm(initial_state)
initial_state =initial_state/magnitude

stepsnumber = 5;
action()

# put x back and recentered the gaussian

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